

## Quick Review of Last Week's Computational Concepts

- ▶ Objects
- ▶ Functions manipulating objects
- ▶ Data frames
- ▶ Vectors
- ▶ Numeric, Character, Boolean, and Factor objects...

## Extra Credit

Goal: change all of the "EE" entries in the ponds data to "E"  
So, after last class, you may try to do this:

```
##### Extra Credit

# this won't work
ponds$site[which(ponds$site == "EE")] <- "E"

## Warning: invalid factor level, NAs generated
```

## What is a factor?

```
ponds$site[1:20]

## [1] A B C D EE A B C D EE A B C D EE A B C
## [19] D EE
## Levels: A B C D EE
```

- ▶ A factor is made up of text strings
- ▶ A factor has levels

## Numerics, Characters, and Factors

```
# a numeric vector
c(1, 2, 3)

## [1] 1 2 3
```

```
# a character vector
c("1", "2", "3")

## [1] "1" "2" "3"
```

```
# a character vector -> factor
factor(c("1", "2", "3"))

## [1] 1 2 3
## Levels: 1 2 3
```

## From Factors to Characters and Back

```
# instead, you need to do this...
ponds$site <- as.character(ponds$site)

ponds$site[which(ponds$site == "EE")] <- "E"

ponds$site <- factor(ponds$site)
```

## Or Just Change Factor Levels...

```
# Or, just change the levels
levels(ponds$site)

## [1] "A" "B" "C" "D" "EE"

levels(ponds$site) <- c("A", "B", "C", "D", "E")

levels(ponds$site)

## [1] "A" "B" "C" "D" "E"
```

## A More Foolproof Level Change...

```
# alternative approach
levels(ponds$site) <- c(levels(ponds$site)[1:4], "E")

ponds$site[1:10]

## [1] A B C D E A B C D E
## Levels: A B C D E
```

You could use which

## Exercise

- ▶ Create a factor vector of the letters A through D that repeats 10 times (use rep)
- ▶ Do the same thing, but with the strings A1, B1, ...D1
- ▶ Merge these two into a single vector.

## Exercise

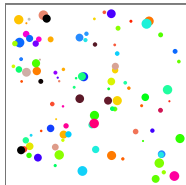
```
# alternative approach
v1 <- factor(rep(c("A", "B", "C", "D"), 10))
v2 <- factor(rep(c("A1", "B1", "C1", "D1"), 10))
v3 <- factor(c(as.character(v1), as.character(v2)))
v3[1:20]

## [1] A B C D A B C D A B C D A B C D A B C D
## Levels: A A1 B B1 C C1 D D1
```

Questions?

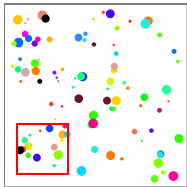
## Sampling Populations

What is a population?



Population = All Individuals

## What is a sample?

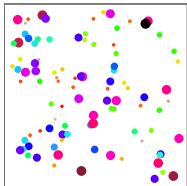


A **sample** of individuals in a randomly distributed population.

## How can sampling a population go awry?

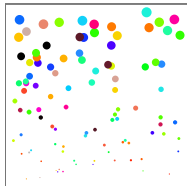
- ▶ Sample is not **representative**
- ▶ Replicates do not have **equal chance** of being sampled
- ▶ Replicates are not **independent**

## Bias from Unequal Representation



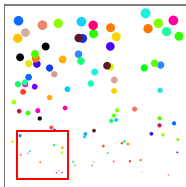
If you only chose one color, you would only get one range of sizes.

## Bias from Unequal Change of Sampling



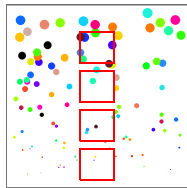
Spatial gradient in size

## Bias from Unequal Change of Sampling



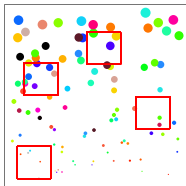
Oh, I'll just grab those individuals closest to me...

## Solution: **Stratified** Sampling



Sample over a known gradient, aka **cluster sampling**  
Can incorporate multiple gradients

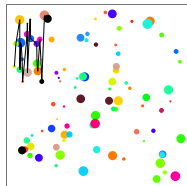
## Solution: Random Sampling



Two sampling schemes:

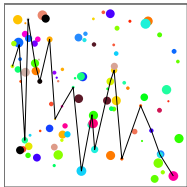
- ▶ **Random** - samples chosen using random numbers
- ▶ **Haphazard** - samples chosen without any system (careful!)

## Non-Independence & Haphazard Sampling



What if there are interactions between individuals?

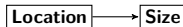
## Solution: Chose Samples Randomly



Path chosen with random number generator

## Deciding Sampling Design

What influences the measurement you are interested in?



Causal Graph

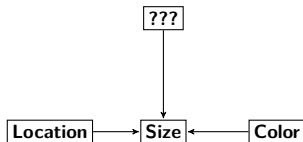
## Stratified or Random?

Do you know all of the influences?



## Stratified or Random?

Do you know all of the influences?



You can represent this as an equation:

$$\text{Size} = \text{Color} + \text{Location} + \text{???}$$

## Stratified or Random?

- ▶ How is your population defined?
- ▶ What is the scale of your inference?
- ▶ What might influence the inclusion of a replicate?
- ▶ How important are external factors you know about?
- ▶ How important are external factors you cannot assess?

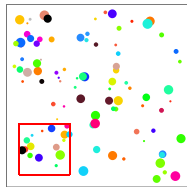
## Exercise

Draw a causal graph of the influences on one thing you measure

How would you sample your population?

## Describing a Sample

## Sample Properties: Mean



What is the mean size of individuals in this population?

$$\bar{y} = \frac{\sum y_i}{n}$$

## Sample Properties: Mean

$$\bar{Y} = \frac{\sum_{i=1}^n y_i}{n}$$

$\bar{Y}$  - The average value of a sample

$x_i$  - The value of a measurement for a single individual

$n$  - The number of individuals in a sample

$\mu$  - The average value of a population  
(Greek = population, Latin = Sample)

## R: Sample Size and Estimate Precision

*As n increases, does your estimate get closer to the true mean?*

1. Taking a mean

```
mean(c(1, 4, 5, 10, 15))  
## [1] 7
```

## R: Sample Size and Estimate Precision

*As n increases, does your estimate get closer to the true mean?*

2. Mean from a random population

```
mean(runif(n = 500, min = 0, max = 100))  
## [1] 47.53
```

*runif* draws from a Uniform distribution

## R: Sample Size and Estimate Precision

*As n increases, does your estimate get closer to the true mean?*

3. Sampling from a simulated population

```
set.seed(5000)  
population <- runif(400, 0, 100)  
mean(sample(population, size = 50))  
## [1] 46.83
```

*set.seed* ensures that you get the same random number every time  
*sample* draws a sample of a defined size from a vector



## Exercise: Sample Size and Estimate Precision

As  $n$  increases, does your estimate get closer to the true mean?

1. Use `runif` (or `rnorm`, if you're feeling saucy) to simulate a population
2. How does the repeatability of the mean change as you change the sample size?

## Exercise: Sample Size and Estimate Precision

As  $n$  increases, does your estimate get closer to the true mean?

```
set.seed(5000)
population <- runif(n = 400, min = 0, max = 100)
mean(sample(population, size = 3))

## [1] 64.52

mean(sample(population, size = 3))

## [1] 54.91
```

## Exercise: Sample Size and Estimate Precision

As  $n$  increases, does your estimate get closer to the true mean?

```
mean(sample(population, size = 100))

## [1] 45.06

mean(sample(population, size = 100))

## [1] 45.96
```

## Sample Properties: Variance

How variable was that population?

$$s^2 = \frac{\sum_{i=1}^n (Y_i - \bar{Y})^2}{n-1}$$

- ▶ **Sums of Squares** over  $n-1$
- ▶  $n-1$  corrects for both sample size and sample bias
- ▶  $\sigma^2$  if describing the population
- ▶ Units in square of measurement...

## Sample Properties: Standard Deviation

$$s = \sqrt{s^2}$$

- ▶ Units the same as the measurement
- ▶ If distribution is normal, 67% of data within 1 SD, 95% within 2
- ▶  $\sigma$  if describing the population

## Exercise: Sample Size and Estimated Sample Variation

1. Repeat the last exercise, but with the functions `sd` or `var`
2. Do you need as many samples for a precise estimate as for the mean?

## Next time...

